



Digital Support for Teachers'
Collaborative Reflection on
Mathematics Classroom Situations

Vignettes
in pre-service teacher education and
in-service teacher professional development

Collection of the

Publications related to

the project coReflect@maths



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Publications related to

the project coReflect@maths

2020

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